PHASE_VOLTAGE		PI	hase Voltage Reconstruction		
Description	This software module calculates three phase voltages impressing to the 3-ph electric motor (i.e., induction or synchronous motor) by using the conventional voltage-source inverter. Three phase voltages can be reconstructed from the DC-bus voltage and three switching functions of the upper power switching devices in the inverter. In addition, this software module also includes the clarke transformation changing from three phase voltages into two stationary dq-axis phase voltages.				
	MfuncV2 MfuncV2 MfuncV3 DcBusV0	► TAGE_CALC			
Availability	This IQ module is available in one interface format:				
	1) The C interface	e version			
Module Properties	Type: Target Independent, Application Dependent				
	Target Devices: x281x or x280x				
	C Version File Names: volt_calc.c, volt_calc.h				
	IQmath library files for C: IQmathLib.h, IQmath.lib				
	Item	C version	Comments		
	Code Size <sup>□</sup> (x281x/x280x)	144/144 words			
	Data RAM	0 words <sup>•</sup>			
	xDAIS ready	No			
	XDAIS component	No	IALG layer not implemented		

 $^{\bullet}$  Each pre-initialized "\_iq" PHASEVOLTAGE structure consumes 22 words in the data memory

<sup>□</sup> Code size mentioned here is the size of the *calc()* function

Yes

Yes

Multiple instances

Reentrancy

C Interface

## **C** Interface

## **Object Definition**

The structure of PHASEVOLTAGE object is defined by following structure definition

typedef struct	_iq MfuncV1; _iq MfuncV2; _iq MfuncV3; Uint32 OutOfPhase; _iq VphaseA; _iq VphaseB; _iq VphaseC; _iq Valpha; _iq Vbeta; void (*calc)();	<ul> <li>// Input: DC-bus voltage</li> <li>// Input: Modulation voltage phase A</li> <li>// Input: Modulation voltage phase B</li> <li>// Input: Modulation voltage phase C</li> <li>// Parameter: Out of Phase adjustment (0 or 1)</li> <li>// Output: Phase voltage phase A</li> <li>// Output: Phase voltage phase B</li> <li>// Output: Phase voltage phase C</li> <li>// Output: Stationary d-axis phase voltage</li> <li>// Output: Stationary q-axis phase voltage</li> <li>// Pointer to calculation function</li> </ul>
	} PHASEVOLTAGE;	

typedef PHASEVOLTAGE \* PHASEVOLTAGE\_handle;

ltem	Name	Description	Format	Range(Hex)
Inputs	DcBusVolt	DC-bus voltage	GLOBAL_Q	8000000-7FFFFFFF
	MfuncV1	Switching function of upper switching device 1	GLOBAL_Q	8000000-7FFFFFF
	MfuncV2	Switching function of upper switching device 2	GLOBAL_Q	80000000-7FFFFFFF
	MfuncV3	Switching function of upper switching device 3	GLOBAL_Q	80000000-7FFFFFFF
Outputs	VphaseA	Line-neutral phase voltage A	GLOBAL_Q	8000000-7FFFFFFF
	VphaseA	Line-neutral phase voltage A	GLOBAL_Q	8000000-7FFFFFFF
	VphaseA	Line-neutral phase voltage A	GLOBAL_Q	80000000-7FFFFFFF
	Valpha	Stationary d-axis phase voltage	GLOBAL_Q	80000000-7FFFFFFF
	Vbeta	Stationary q-axis phase voltage	GLOBAL_Q	8000000-7FFFFFFF

GLOBAL\_Q valued between 1 and 30 is defined in the IQmathLib.h header file.

## Special Constants and Data types

## PHASEVOLTAGE

The module definition is created as a data type. This makes it convenient to instance an interface to phase voltage reconstruction. To create multiple instances of the module simply declare variables of type PHASEVOLTAGE.

## PHASEVOLTAGE\_handle

User defined Data type of pointer to PHASEVOLTAGE module

## PHASEVOLTAGE\_DEFAULTS

Structure symbolic constant to initialize PHASEVOLTAGE module. This provides the initial values to the terminal variables as well as method pointers.

## Methods

#### void phase\_voltage\_calc(PHASEVOLTAGE\_handle);

This definition implements one method viz., the phase voltage reconstruction computation function. The input argument to this function is the module handle.

## Module Usage

#### Instantiation

The following example instances two PHASEVOLTAGE objects PHASEVOLTAGE volt1, volt2;

#### Initialization

To Instance pre-initialized objects PHASEVOLTAGE volt1 = PHASEVOLTAGE\_DEFAULTS; PHASEVOLTAGE volt2 = PHASEVOLTAGE\_DEFAULTS;

# **Invoking the computation function** volt1.calc(&volt1);

```
volt2.calc(&volt2);
```

#### Example

The following pseudo code provides the information about the module usage.

main() {

# }

void interrupt periodic\_interrupt\_isr()

#### {

```
volt1.DcBusVolt = dc volt1:
                                        // Pass inputs to volt1
volt1.MfuncV1 = M1_1;
                                       // Pass inputs to volt1
volt1.MfuncV2 = M2 1;
                                       // Pass inputs to volt1
volt1.MfuncV3 = M3 1;
                                       // Pass inputs to volt1
volt2.DcBusVolt = dc volt2;
                                        // Pass inputs to volt2
volt2.MfuncV1 = M1_2;
                                        // Pass inputs to volt2
                                        // Pass inputs to volt2
volt2.MfuncV2 = M2_2;
volt2.MfuncV3 = M3 2;
                                        // Pass inputs to volt2
volt1.calc(&volt1);
                                        // Call compute function for volt1
                                        // Call compute function for volt2
volt2.calc(&volt2);
Vd1 = volt1.Valpha;
                                         // Access the outputs of volt1
Vq1 = volt1.Vbeta;
                                        // Access the outputs of volt1
Vd2 = volt2.Valpha;
                                        // Access the outputs of volt2
                                        // Access the outputs of volt2
Vq2 = volt2.Vbeta;
```

#### }

## **Technical Background**

The phase voltage of a general 3-ph motor ( $V_{an}$ ,  $V_{bn}$ , and  $V_{cn}$ ) can be calculated from the DC-bus voltage ( $V_{dc}$ ) and three upper switching functions of inverter ( $S_1$ ,  $S_2$ , and  $S_3$ ). The 3-ph windings of motor are connected as the Y connection without a neutral return path (or 3-ph, 3-wire system). The overall system can be shown in Figure 1.

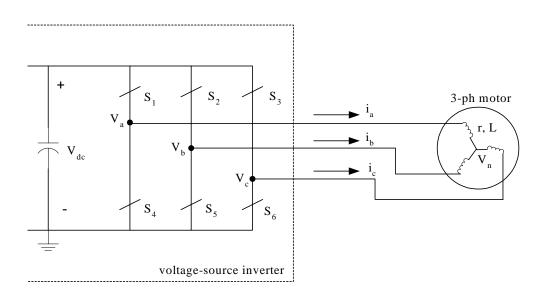


Figure 1: Voltage-source inverter with a 3-ph electric motor

Each phase of the motor is simply modeled as a series impedance of resistance and inductance (r, L) and back emf ( $e_a$ ,  $e_b$ ,  $e_c$ ). Thus, three phase voltages can be computed as

$$V_{an} = V_a - V_n = i_a r + L \frac{di_a}{dt} + e_a$$
(1)

$$V_{bn} = V_b - V_n = i_b r + L \frac{di_b}{dt} + e_b$$
 (2)

$$V_{cn} = V_{c} - V_{n} = i_{c}r + L\frac{di_{c}}{dt} + e_{c}$$
 (3)

Summing these three phase voltages, yields

$$V_{a} + V_{b} + V_{c} - 3V_{n} = (i_{a} + i_{b} + i_{c})r + L\frac{d(i_{a} + i_{b} + i_{c})}{dt} + e_{a} + e_{b} + e_{c}$$
(4)

Without a neutral return path, according to KCL, i.e.,  $i_a + i_b + i_c = 0$ , and the back emfs are balanced and symmetrical due to the 3-ph winding structures, i.e.,  $e_a + e_b + e_c = 0$ , so (4) becomes

$$\mathbf{V}_{\mathrm{an}} + \mathbf{V}_{\mathrm{bn}} + \mathbf{V}_{\mathrm{cn}} = \mathbf{0} \tag{5}$$

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Furthermore, the neutral voltage can be simply derived from (4)-(5) as

$$V_{n} = \frac{1}{3} (V_{a} + V_{b} + V_{c})$$
 (6)

Now three phase voltages can be calculated as

$$V_{an} = V_{a} - \frac{1}{3} (V_{a} + V_{b} + V_{c}) = \frac{2}{3} V_{a} - \frac{1}{3} V_{b} - \frac{1}{3} V_{c}$$
(7)

$$V_{bn} = V_{b} - \frac{1}{3} (V_{a} + V_{b} + V_{c}) = \frac{2}{3} V_{b} - \frac{1}{3} V_{a} - \frac{1}{3} V_{c}$$
(8)

$$V_{cn} = V_{c} - \frac{1}{3} (V_{a} + V_{b} + V_{c}) = \frac{2}{3} V_{c} - \frac{1}{3} V_{a} - \frac{1}{3} V_{b}$$
(9)

Three voltages  $V_a$ ,  $V_b$ ,  $V_c$  are related to the DC-bus voltage ( $V_{dc}$ ) and three upper switching functions ( $S_1$ ,  $S_2$ ,  $S_3$ ) as the following relation.

$$\mathbf{V}_{a} = \mathbf{S}_{1} \mathbf{V}_{dc} \tag{10}$$

$$\mathbf{V}_{\rm h} = \mathbf{S}_2 \mathbf{V}_{\rm dc} \tag{11}$$

$$\mathbf{V}_{c} = \mathbf{S}_{3} \mathbf{V}_{dc} \tag{12}$$

where 
$$S_1$$
,  $S_2$ ,  $S_3$  = either 0 or 1, and  $S_4$  = 1- $S_1$ ,  $S_5$  = 1- $S_2$ , and  $S_6$  = 1- $S_3$ . (13)

As a result, three phase voltages in (7)-(9) can also be expressed in terms of DC-bus voltage and three upper switching functions as follows:

$$\mathbf{V}_{an} = \mathbf{V}_{dc} \left( \frac{2}{3} \mathbf{S}_1 - \frac{1}{3} \mathbf{S}_2 - \frac{1}{3} \mathbf{S}_3 \right)$$
(14)

$$\mathbf{V}_{bn} = \mathbf{V}_{dc} \left( \frac{2}{3} \mathbf{S}_2 - \frac{1}{3} \mathbf{S}_1 - \frac{1}{3} \mathbf{S}_3 \right)$$
(15)

$$\mathbf{V}_{cn} = \mathbf{V}_{dc} \left( \frac{2}{3} \mathbf{S}_3 - \frac{1}{3} \mathbf{S}_1 - \frac{1}{3} \mathbf{S}_2 \right)$$
(16)

It is emphasized that the  $S_1$ ,  $S_2$ , and  $S_3$  are defined as the upper switching functions. If the lower switching functions are available instead, then the out-of-phase correction of switching functions is required in order to get the upper switching functions as easily computed from equation (13).

Next the clarke transformation changing from three phase voltages (V<sub>an</sub>, V<sub>bn</sub>, and V<sub>cn</sub>) to the stationary dq-axis phase voltages ( $V_{ds}^{s}$ , and  $V_{qs}^{s}$ ) are applied by using the following relationship. Because of the balanced system (5), V<sub>cn</sub> is not used in clarke transformation.

$$V_{\rm ds}^{\rm s} = V_{\rm an} \tag{17}$$

$$V_{qs}^{s} = \frac{1}{\sqrt{3}} \left( V_{an} + 2V_{bn} \right)$$
(18)

Figure 2 depicts the abc-axis and stationary dq-axis components for the stator voltages of motor. Notice that the notation of the stationary dq-axis is sometimes used as the stationary  $\alpha\beta$ -axis, accordingly.

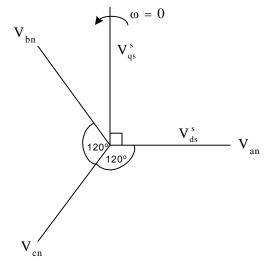


Figure 2: The abc-axis and stationary dq-axis components of the stator phase voltages

Next, Table 1 shows the correspondence of notations between variables used here and variables used in the program (i.e., volt\_calc.c, volt\_calc.h). The software module requires that both input and output variables are in per unit values.

	Equation Variables	Program Variables
Inputs	S <sub>1</sub>	MfuncV1
	S <sub>2</sub>	MfuncV2
	S <sub>3</sub>	MfuncV3
	V <sub>dc</sub>	DcBusVolt
Outputs	V <sub>an</sub>	VphaseA
	V <sub>bn</sub>	VphaseB
	V <sub>cn</sub>	VphaseC
	$V^{s}_{ds}$	Valpha
	$V_{qs}^{s}$	Vbeta

Table 1: Correspondence of notations